

Statistical Collusion by Collectives on Learning Platforms

Etienne Gauthier, Francis Bach, Michael I. Jordan
(INRIA, Ecole Normale Supérieure)

Numerous examples of collectives
emerging to strategically influence
platforms



BUSINESS INSIDER

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The Geotagging Counterpublic:

The Case of Facebook Remote Check-Ins to Standing Rock

- Facebook users relocalized themselves to Standing Rock to disrupt surveillance and blur police tracking

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[Home](#)

How Neighborhoods Are Fighting Off Traffic That Waze Sends Their Way

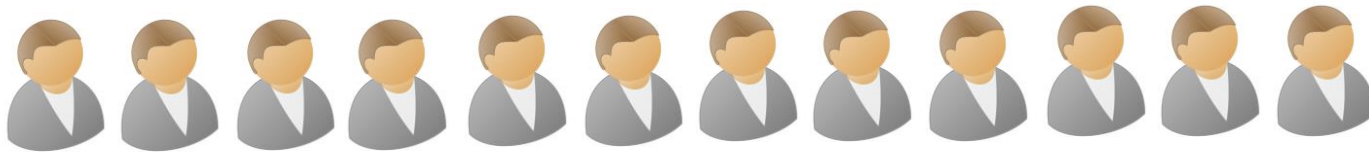
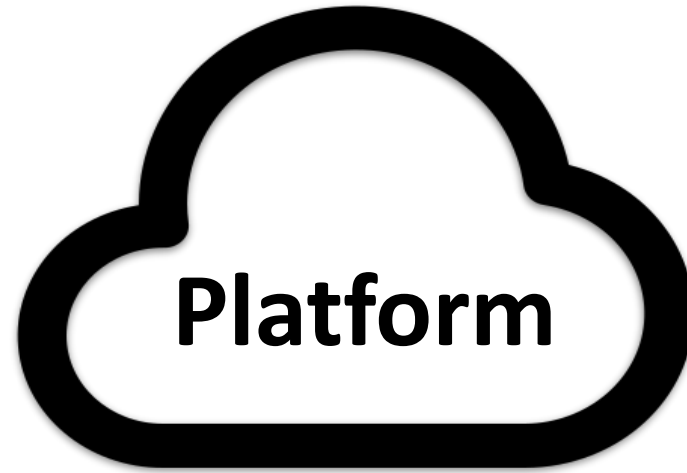
When Waze or Google Maps turns your sleepy street into a veritable highway, you don't just have to sit there and take it.

- Waze users falsely report accidents to keep traffic out of their neighborhoods

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Model

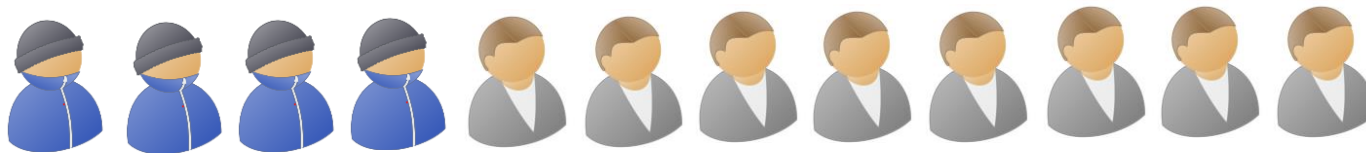
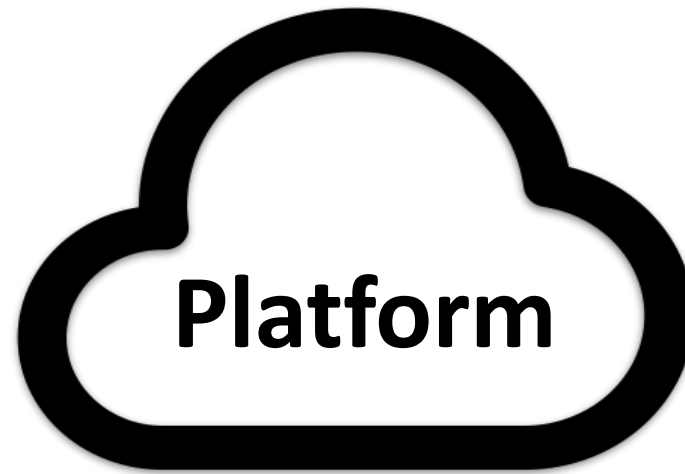
Initially, each user is drawn from the same probability distribution \mathcal{D} over feature-label pairs $X \times Y$



N consumers $\overset{\text{i.i.d.}}{\sim} \mathcal{D}$

Model

A collective forms to influence
the platform's behavior toward
a shared goal



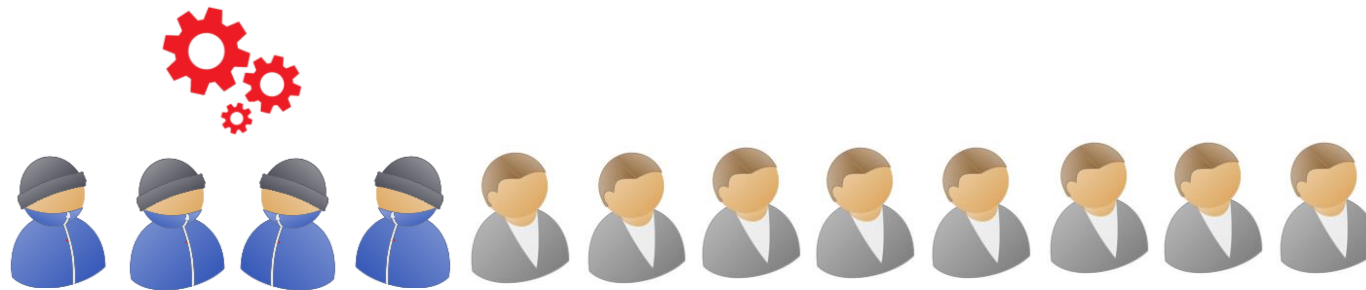
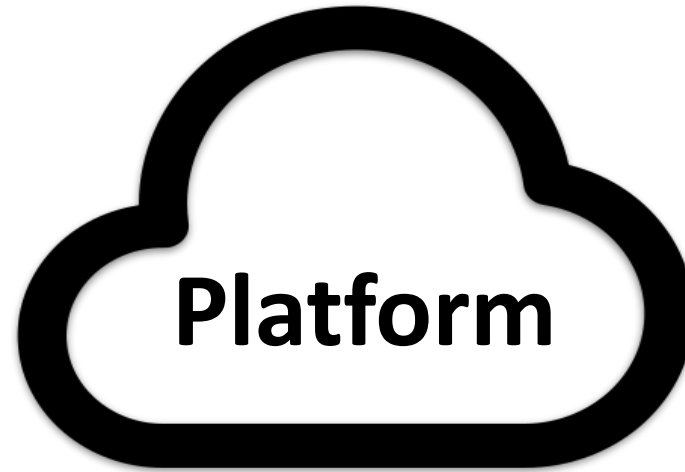
Collective
(size n)

Rest of the population
(size $N - n$)

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Model

Collective members share their data to identify effective strategies and anticipate their influence on the platform



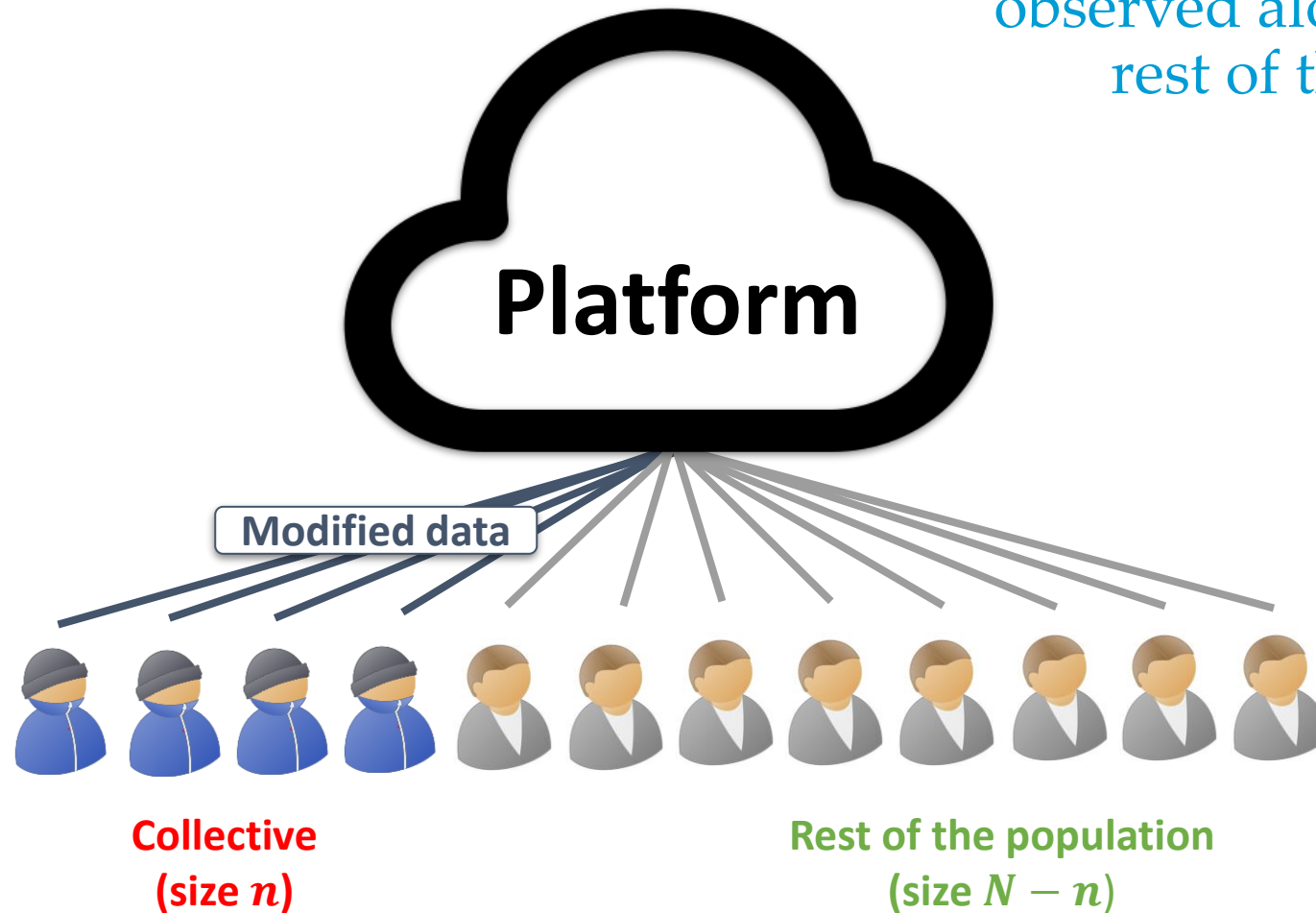
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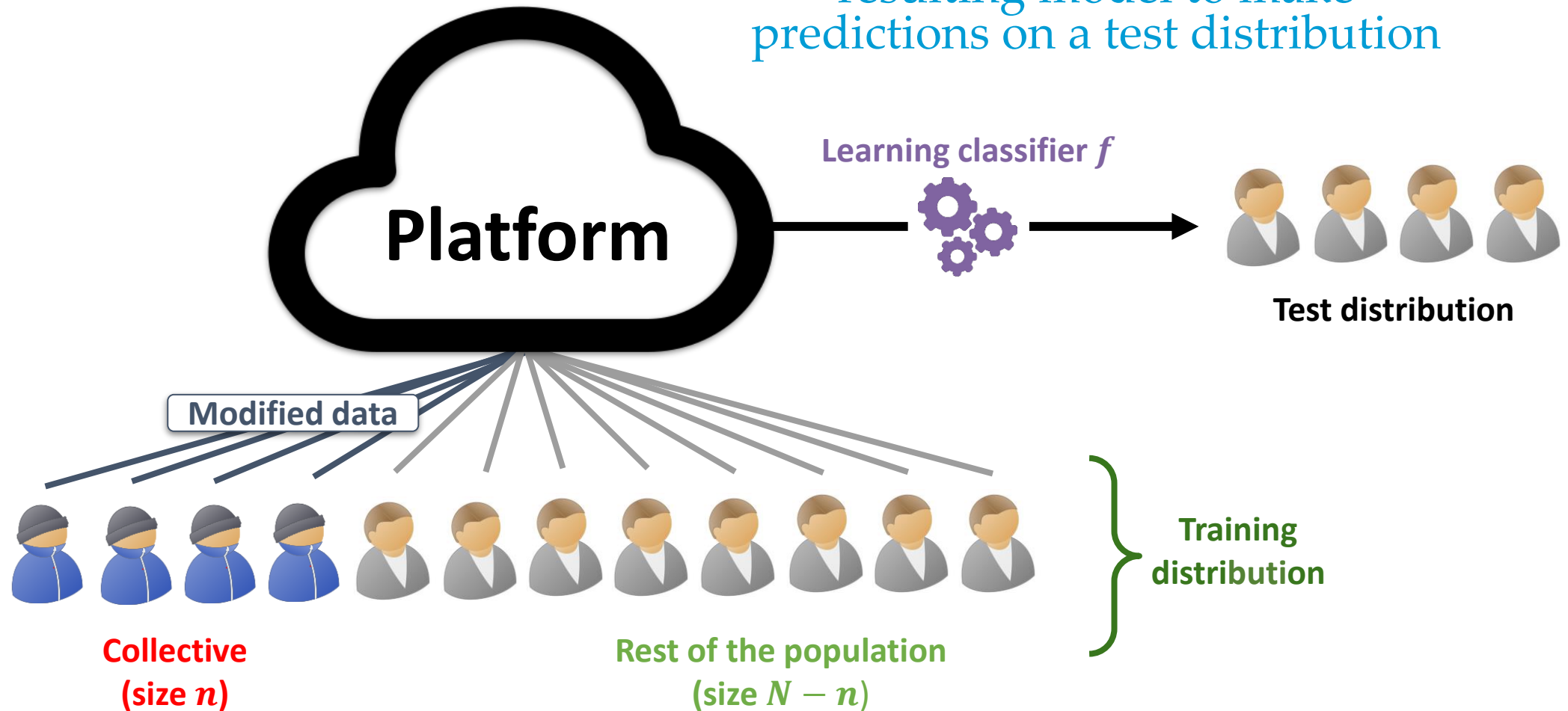
Model

Collective members modify their data, which is then observed alongside that of the rest of the population



Model

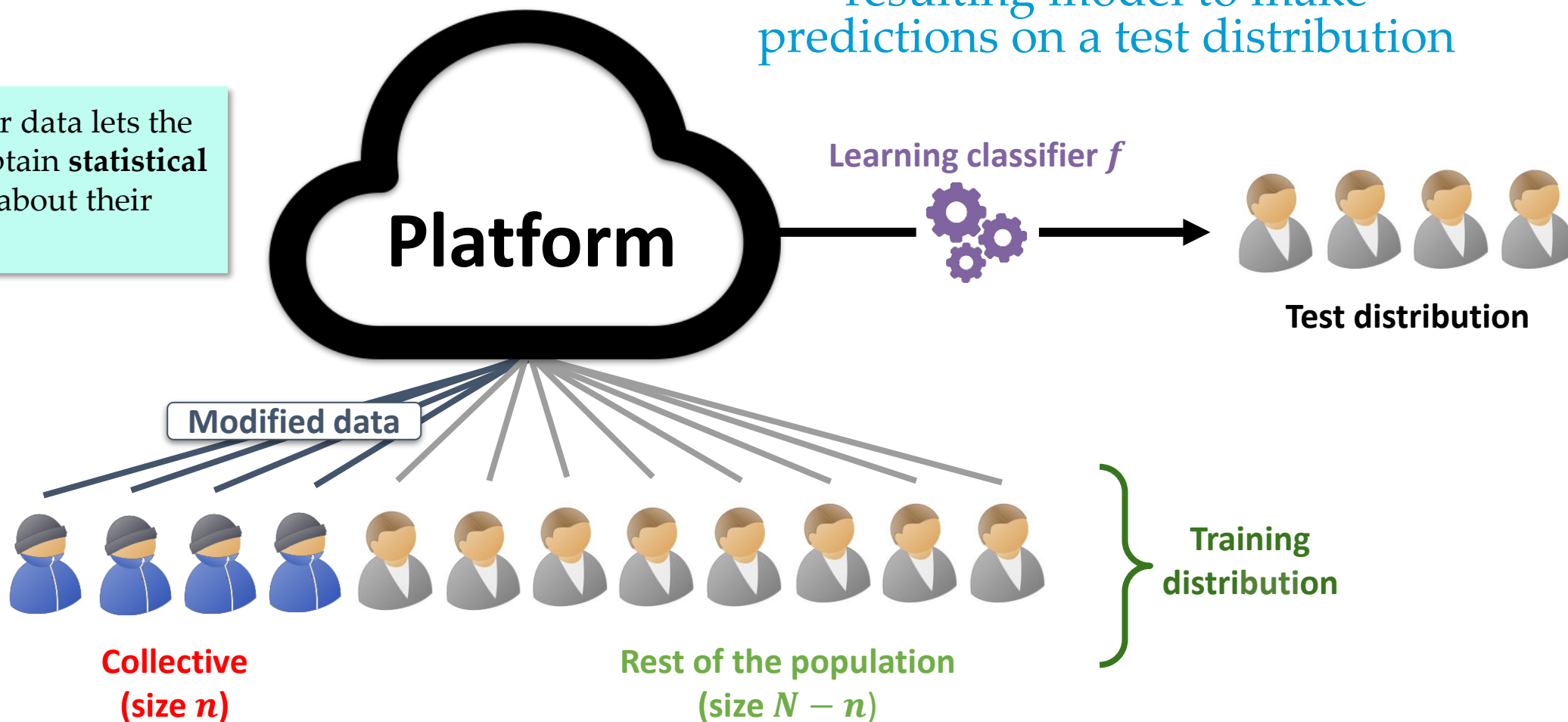
The platform learns from the training data and uses the resulting model to make predictions on a test distribution



Model

- Pooling their data lets the collective obtain **statistical guarantees** about their impact

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Platform's behavior

$$f(x) = \operatorname{argmax}_y \mathcal{P}(y|x)$$

[Hardt et al., 2023]

Space of probability
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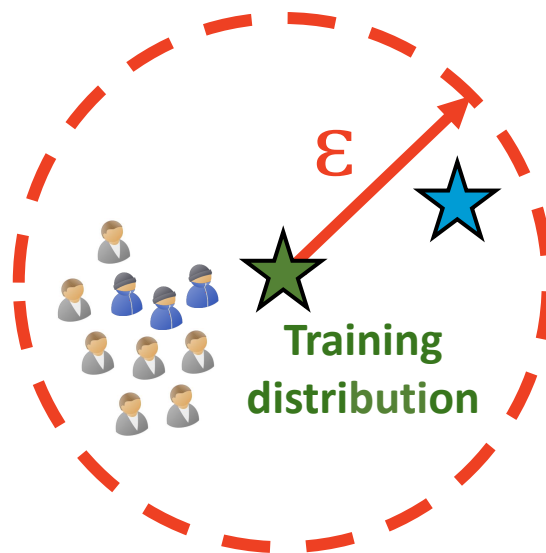


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Maximize a measure of success $S(n)$

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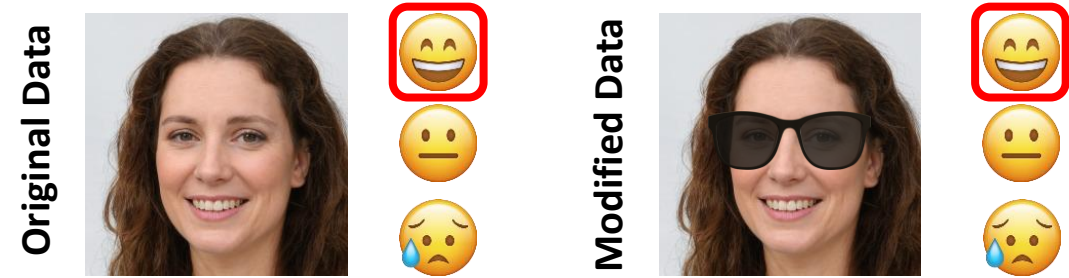
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➤ **Results:** for each objective, we analyze **strategies** that the collective can set and we derive **strategy-dependent high-probability lower bounds** on $S(n)$

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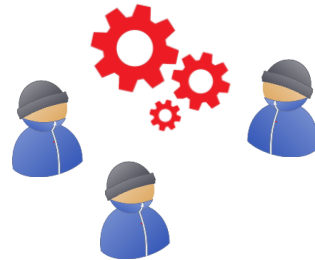
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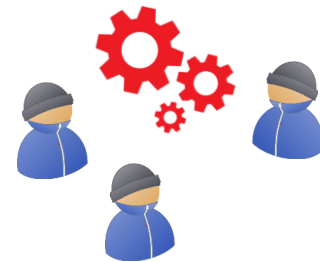


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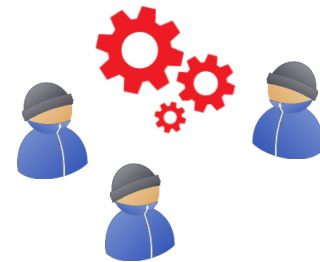
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Platform robustness ($\nearrow \epsilon$)

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Experiments



Synthetic Dataset: Car Evaluation

- **Features:** 18 attributes including *Model Type*, *Fuel Type*, *Country of Manufacture*, etc.
- **Labels (4 classes):** Excellent, Good, Average, Poor

Experiments



Synthetic Dataset: Car Evaluation

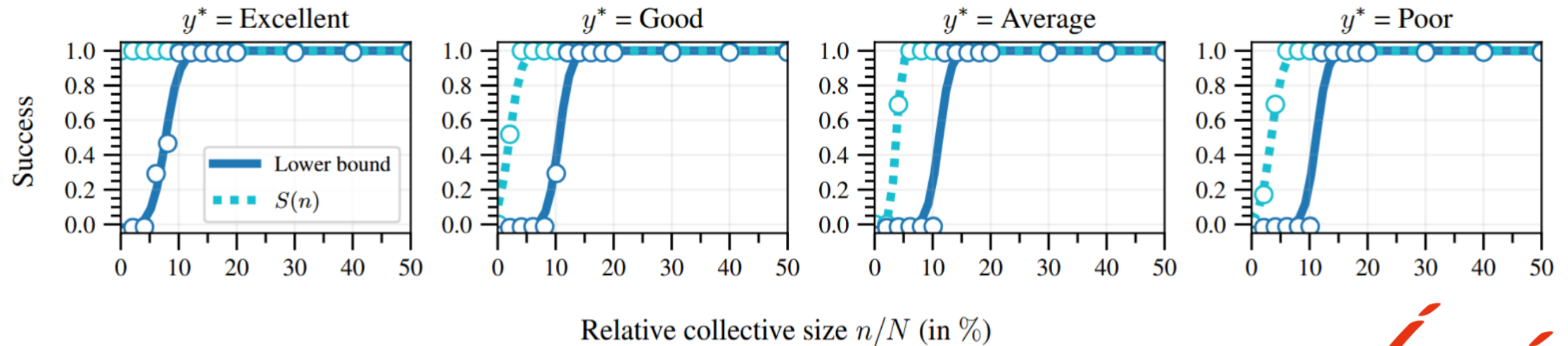
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Beyond This Talk: What's in the Paper

- ❑ **General Framework:** formal modelization
- ❑ **Different Objectives:** signal planting, unplanting, and erasing
- ❑ **More Strategies:** feature-label vs feature-only, adaptive vs static
- ❑ **Theory:** explicit lower bounds, algorithmic implementations
- ❑ **Parameters Influence:** how impact varies with collective size n and number of consumers N
 - platforms interacting with large user bases are more exposed to collectives altering their data

Conclusion

- ❑ By **sharing their data**, collectives can **infer** and put into practice impactful strategies
- ❑ Our approach enables collectives to **anticipate their potential impact** on learning platforms
- ❑ Opens new directions for understanding **multi-agent influence** on learning platforms

Thank you! Questions?

Poster:

📌 East Exhibition Hall

A-B #E-700

🕒 4:30 to 7:00 PM

Paper



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